
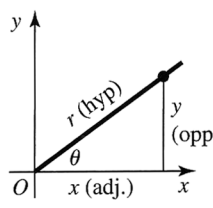
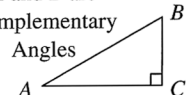
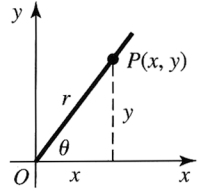
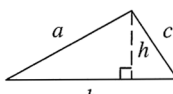
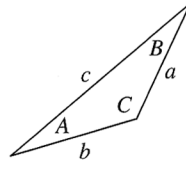



RIGHT TRIANGLES		Pythagorean Theorem	$a^2 + b^2 = c^2$		
	<p>Trigonometric Ratios</p> 	Sine	$\sin \theta = \frac{y}{r} = \frac{\text{opposite side}}{\text{hypotenuse}}$		
		Cosine	$\cos \theta = \frac{x}{r} = \frac{\text{adjacent side}}{\text{hypotenuse}}$		
		Tangent	$\tan \theta = \frac{y}{x} = \frac{\text{opposite side}}{\text{adjacent side}}$		
		Cotangent	$\cot \theta = \frac{x}{y} = \frac{\text{adjacent side}}{\text{opposite side}}$		
		Secant	$\sec \theta = \frac{r}{x} = \frac{\text{hypotenuse}}{\text{adjacent side}}$		
		Cosecant	$\csc \theta = \frac{r}{y} = \frac{\text{hypotenuse}}{\text{opposite side}}$		
Reciprocal Relations	(a) $\csc \theta = \frac{1}{\sin \theta}$	(b) $\sec \theta = \frac{1}{\cos \theta}$	(c) $\cot \theta = \frac{1}{\tan \theta}$		
<p>A and B are Complementary Angles</p> 	Cofunctions	(a) $\sin A = \cos B$ (b) $\cos A = \sin B$ (c) $\tan A = \cot B$	(d) $\cot A = \tan B$ (e) $\sec A = \csc B$ (f) $\csc A = \sec B$		
COORDINATE SYSTEMS		Rectangular	$x = r \cos \theta$		
			$y = r \sin \theta$		
		Polar	$r = \sqrt{x^2 + y^2}$		
			$\theta = \arctan \frac{y}{x}$		
ANY TRIANGLE	<p>Areas</p> 	Area = $\frac{1}{2}bh$			
		Hero's Formula:	Area = $\sqrt{s(s-a)(s-b)(s-c)}$ where $s = \frac{1}{2}(a+b+c)$		
		Sum of the Angles	$A + B + C = 180^\circ$		
		Law of Sines	$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$		
		Law of Cosines	$a^2 = b^2 + c^2 - 2bc \cos A$ $b^2 = a^2 + c^2 - 2ac \cos B$ $c^2 = a^2 + b^2 - 2ab \cos C$		
	Exterior Angle	$\theta = A + B$			
SIMILAR TRIANGLES	If two angles of a triangle equal two angles of another triangle, the triangles are similar.				
	Corresponding sides of similar triangles are in proportion.				

## Basic Rules of Algebra for real numbers

Assume  $a, b, c, d$  are real numbers and that  $m, n$  are positive integers.

Commutativity  $a + b = b + a$   $a \cdot b = b \cdot a$

Note:  $a + a = 2a$   $a \cdot a = a^2$

Associativity  $a + (b + c) = (a + b) + c$   $a \cdot (b \cdot c) = (a \cdot b) \cdot c$

Distributive law  $a(b + c) = ab + ac$

Note:  $(a + b)(c + d) = (a + b)c + (a + b)d = ac + bc + ad + bd$

### Factoring Special Polynomials:

Perfect Squares  $a^2 - 2ab + b^2 = (a - b)^2$   $a^2 + 2ab + b^2 = (a + b)^2$

Difference of Squares  $a^2 - b^2 = (a - b)(a + b)$

Difference/Sum of Cubes  $a^3 - b^3 = (a - b)(a^2 + ab + b^2)$   $a^3 + b^3 = (a + b)(a^2 - ab + b^2)$

Binomial Equation  $(a + b)^n = \sum_{r=0}^n \binom{n}{r} a^{n-r} b^r$  where  $\binom{n}{r} = \frac{n!}{(n-r)!r!}$  and  $m! = m(m-1) \dots 1$  also  $0! = 1$

Identities and Inverses  $a + 0 = a = 0 + a$   $a \cdot 1 = a = 1 \cdot a$

$a + (-a) = 0 = (-a) + a$   $a \cdot \left(\frac{1}{a}\right) = 1 = \left(\frac{1}{a}\right) \cdot a, a \neq 0$

Fractions  $\frac{a}{b} + \frac{c}{d} = \frac{ad}{bd} + \frac{bc}{bd} = \frac{ad+bc}{bd}$   $\frac{a}{b} \cdot \left(\frac{c}{d}\right) = \frac{ac}{bd}$

$\frac{a}{b} + \frac{c}{b} = \frac{a+c}{b}$   $\frac{a}{b} \cdot \left(\frac{c}{b}\right) = \frac{ac}{b^2}$

$a + \frac{b}{c} = \frac{ac}{c} + \frac{b}{c} = \frac{ac+b}{c}$   $a \cdot \left(\frac{b}{c}\right) = \frac{a}{1} \cdot \left(\frac{b}{c}\right) = \frac{ab}{c}$

$\frac{a}{b} - \frac{c}{d} = \frac{a}{b} + \frac{-c}{d} = \frac{ad-bc}{bd}$   $\frac{a}{b} \div \frac{c}{d} = \frac{a}{b} \cdot \frac{d}{c} = \frac{ad}{bc}$

Exponents  $a^0 = 1, a \neq 0$   $0^a = 0, a \neq 0$

$\underbrace{a \cdot a \cdot \dots \cdot a}_{m \text{ times}} = a^m$   $a^{\frac{1}{m}} = \sqrt[m]{a}$

$a^b$  is well defined when  $a$  and  $b$  are not both 0  
(in other words  $0^0$  is not well defined for the purposes of 1<sup>st</sup> and 2<sup>nd</sup> year math courses)

$a^b$  is a complex number if  $a < 0$  and  $b = m\left(\frac{1}{2^n}\right)$   
(in other words the even root of a negative number is not a real number)

$a^b \cdot a^c = a^{b+c}$   $\frac{a^b}{a^c} = a^{b-c}$   $(a^b)^c = a^{bc}$

$(ab)^c = a^c \cdot b^c$   $\left(\frac{a}{b}\right)^c = \frac{a^c}{b^c}$   $\left(\frac{a}{b}\right)^{-c} = \frac{a^{-c}}{b^{-c}} = \frac{b^c}{a^c} = \left(\frac{b}{a}\right)^c$

$a^b + a^b = 2a^b$  but  $a^b + a^c$  and  $a^b + c^b$  cannot be simplified

Logarithms If  $a = b^c$  then  $c = \log_b a = \frac{\ln a}{\ln b}$ ,  $b > 0$  and  $b \neq 1$ .

$\log_b b^c = c$   $\log_b(a^c) = c \log_b a$

$\log_b(ac) = \log_b a + \log_b c$   $\log_b\left(\frac{a}{c}\right) = \log_b a - \log_b c$

$\log_b(a + a) = \log_b(2a)$  but  $\log_b(a + c)$  cannot be simplified